

LAPACK Working Note 71

IBM RS/6000-550 & -590 Performance for Selected Routines in ESSL*/LAPACK /NAG[†]/IMSL^{‡§}

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1 Overview

This document contains performance results for selected double-precision real and double-precision complex LAPACK routines and their equivalents in ESSL, NAG, and IMSL. The routines are listed in Figure 1.

2 Timing Environments

The experiments were conducted in two different timing environments: the IBM RS/6000-550 and the IBM RS/6000-590. In both cases the input matrices were identical for similar routines from different packages, thereby eliminating timing discrepancies resulting from pivoting, etc. Also, all timings were performed with no other users logged in to the machine.

2.1 IBM RS/6000 model 550

For the RS/6000 model 550 machine, routines were selected from the following four numerical algebra packages:

ESSL Version 2.2.1

*ESSL is a trademark of IBM.

[†]NAG is a trademark of The Numerical Algorithms Group Limited.

[‡]IMSL is a trademark of Visual Numerics, Inc.

[§]This work supported in part by the Office of Scientific Computing, U.S. Department of Energy, under Contract DE-AC05-84OR21400 and in part by IBM.

Figure 1: **The matched subroutines from each library and a brief description. Similar descriptions list the double-precision real routines before the double-precision complex.**

| Description | LAPACK | ESSL | NAG | IMSL |
|-----------------------------------|--------|--------------------|--------|--------|
| General LU Factorization | DGETRF | DGEF | F07ADF | DLFTRG |
| General LU Factorization | ZGETRF | ZGEF | F07ARF | DLFTCG |
| Solve $Ax = b$ Using LU | DGETRS | DGESM | F07AEF | DLFSRG |
| Solve $Ax = b$ Using LU | ZGETRS | ZGESM | F07ASF | DLFSCG |
| Cholesky Factorization | DPOTRF | DPOF | F07FDF | DLFTDS |
| Cholesky Factorization | ZPOTRF | ZPOF | F07FRF | DLFTDH |
| Solve $Ax = b$ Using Cholesky | DPOTRS | DPOSM | F07FEF | DLFSDS |
| Solve $Ax = b$ Using Cholesky | ZPOTRS | ZPOSM | F07FSF | DLFSDH |
| Find Eigenvalues and Eigenvectors | DSPEV | DSLEV ^a | F02ABF | DEVSCF |
| Find Eigenvalues and Eigenvectors | ZHPEV | ZHLEV ^b | F02AXF | DEVSHF |

^aESSL 2.2.1 accepts either DSPEV or DSLEV as the subroutine name for this routine; therefore, DSLEV has been used to prevent a name conflict with LAPACK's DSPEV. This is consistent throughout this report.

^bESSL 2.2.1 accepts either ZHPEV or ZHLEV as the subroutine name for this routine; therefore, ZHLEV has been used to prevent a name conflict with LAPACK's ZHPEV. This is consistent throughout this report.

LAPACK 1.1

NAG Mark 16

IMSL Version 2.0

All of the timings were made under the following conditions:

- AIX 3.2.5 was the operating system.
- XLF 3.1 was the Fortran compiler.
- `xlf -O2 filename.f` was the compile command for **all** subroutines.
- `-lessl` was the ESSL library link for this architecture.
- The BLAS for all packages were supplied by the ESSL library. This gave all the packages an equal footing: that is to say, the algorithmic speed of different routines could be measured without an initial handicap of a slower or naive BLAS implementation.
- `READRTC` was the IBM-supplied utility subprogram for obtaining the timing data. It has a resolution of 1 microsecond.
- Blocksize selection routines were not modified for any of the blocking algorithms in any of the packages.

2.2 IBM RS/6000 model 590–256kByte data cache

For the IBM RS/6000 model 590 machine, routines were selected from the following two numerical algebra packages; IMSL and NAG have not yet been made available for the XLF 3.1 compiler on this architecture.

ESSL Version 2.2.1

LAPACK 1.1

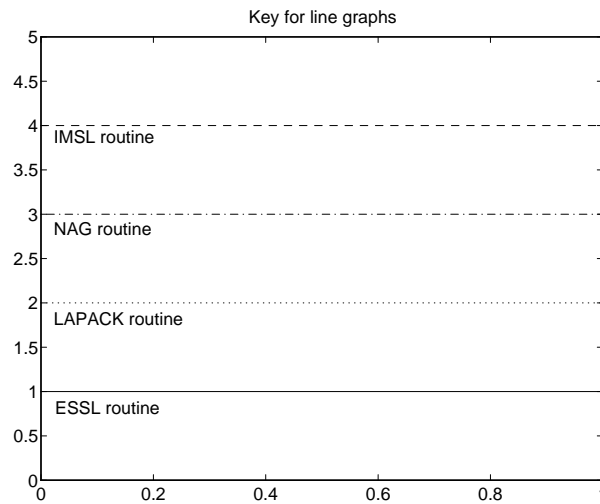
All of the timings were made under the following parameters:

- AIX 3.2.5 was the operating system.
- XLF 3.1 was the Fortran compiler.
- *xf -O2 -qarch=pwrx filename.f* was the compile command for **all** subroutines.
- *-lesslp2* was the ESSL library link for this architecture.
- The BLAS were supplied by the ESSL package. This gave all the packages an equal footing: that is to say, the algorithmic speed of different routines could be measured without an initial handicap of a slower or naive BLAS implementation.
- *READRTC* was the IBM-supplied utility subprogram for obtaining the timing data. It has a resolution of 1 microsecond.
- Blocksize selection routines were not modified for any of the blocking algorithms in any of the packages.

3 Results

In this section, we discuss the computational results for each routine. Also discussed are the tests that were performed to ensure the validity of the timing data, as well as any specifics to the implementation of the subroutine. The title of each subsection is the “4-tuple” of equivalent routines from ESSL, LAPACK, NAG, and IMSL, respectively.

All graphs utilize the following key:



Several points should be noted in reading the graphs:

- The data from both machines is graphed together; therefore, six lines appear on every graph (4 from the 550 and 2 from the 590). When two lines of the same type occur (only ESSL or LAPACK), the “faster” line always represents the IBM RS/6000-590. This format allows the comparison of all the numerical packages on the IBM RS/6000-550 as well as the contrast of ESSL and LAPACK on both machines.
- Some lines may overlap. In case of confusion, the timing data should be consulted.

3.1 *DGEF, DGETRF, F07ADF, DLFTRG*

The four routines *DGEF*, *DGETRF*, *F07ADF*, and *DLFTRG* compute the *LU* factorization of a general square *DOUBLE PRECISION* matrix. Note that NAG's implementation of *F07ADF* is LAPACK's *DGETRF*; consequently, the times are similar. Also, note that *DGEF* produces the same output format as *DGETRF*.

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

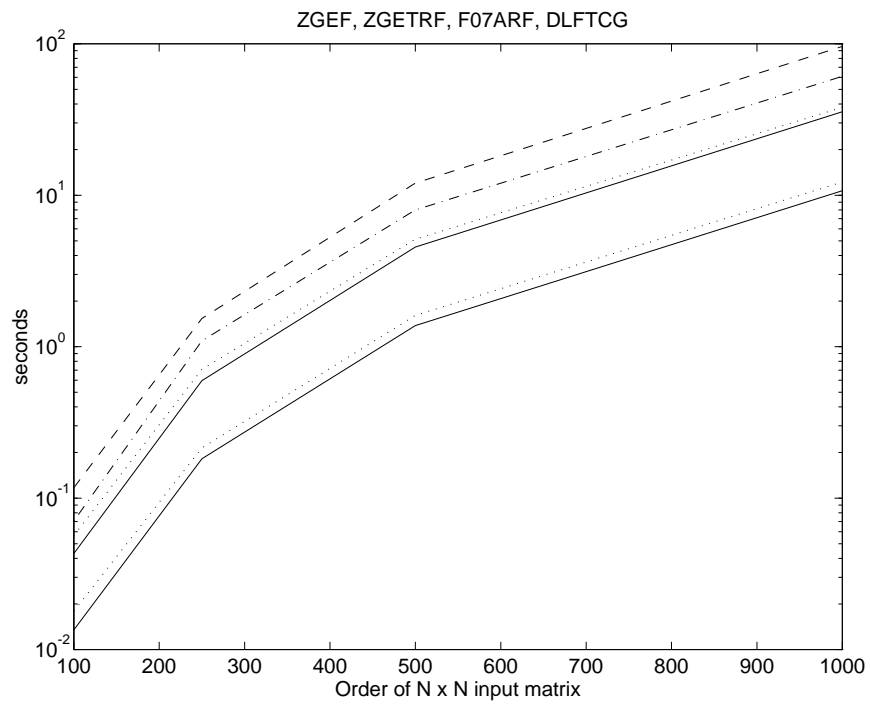
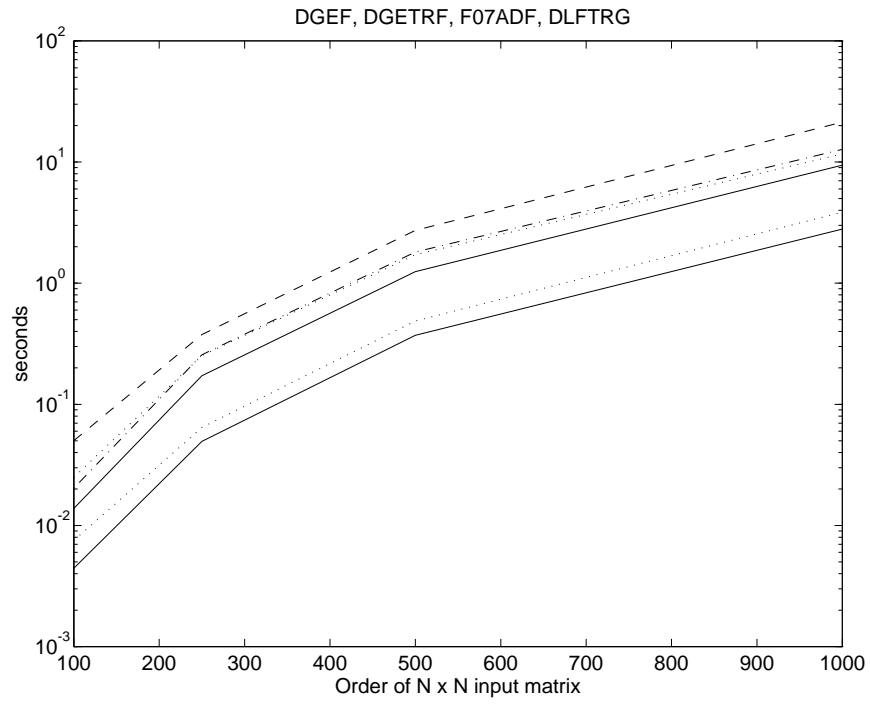
where ϵ is the machine precision.

3.2 *ZGEF, ZGETRF, F07ARF, DLFTCG*

The routines *ZGEF*, *ZGETRF*, *F07ARF*, and *DLFTCG* compute the *LU* factorization of a general square *COMPLEX*16* matrix. Note that NAG's implementation of *F07ARF* is LAPACK's *ZGETRF*; consequently, the times are similar. Also, note that *ZGEF* produces the same output format as *ZGETRF*. The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.



3.3 *DGESM, DGETRS, F07AE, DLFSRG*

The routines *DGESM*, *DGETRS*, *F07AEF*, and *DLFSRG* perform a DOUBLE PRECISION triangular solve, given a solution matrix and the factorization from Section 3.1. Note that NAG's implementation of *F07AEF*, ESSL's implementation of *DGESM*, and LAPACK's implementation of *DGETRS* are essentially the same; consequently, the times are similar. Also, IMSL's routine does not solve for multiple right-hand sides—rather, just a solution vector. Therefore, the following code was used to make IMSL's routine equivalent to the others:

```
DO 100 IRHS = 1, NRHS
  CALL DLFSRG(..., B( 1, IRHS ), ...)
100 CONTINUE
```

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.

3.4 *ZGESM, ZGETRS, F07ASF, DLFSCG*

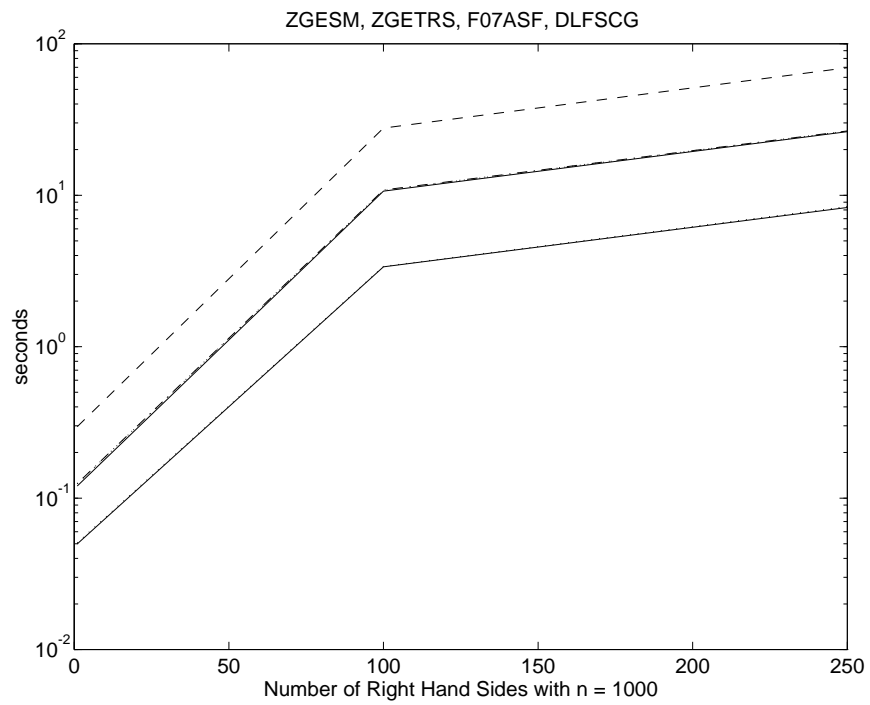
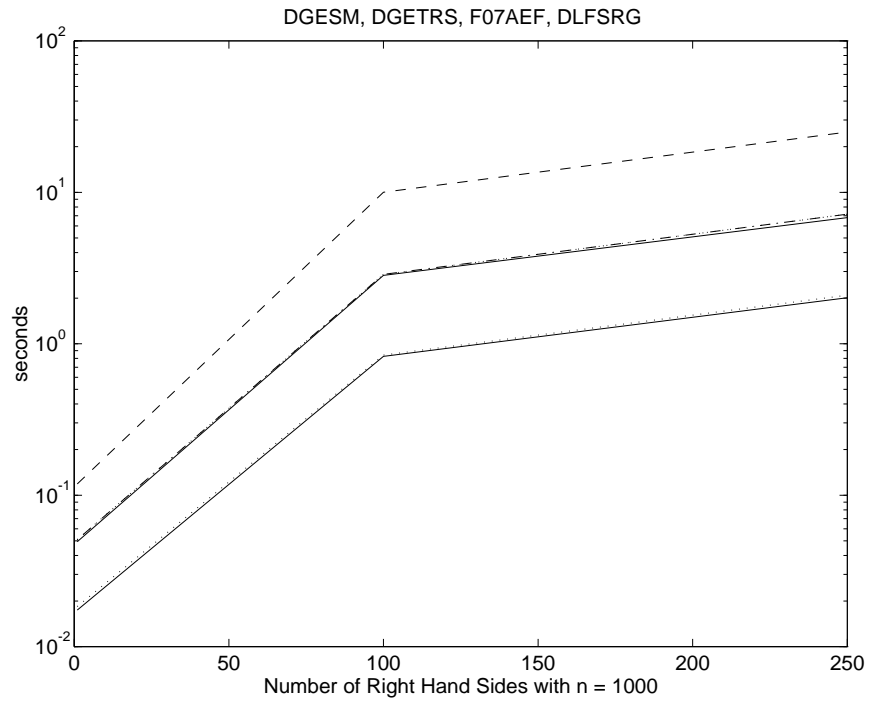
The routines *ZGESM*, *ZGETRS*, *F07ASF*, and *DLFSCG* perform a COMPLEX*16 triangular solve, given a solution matrix and the factorization from Section 3.2. Note that NAG's implementation of *F07ASF*, ESSL's implementation of *ZGESM*, and LAPACK's implementation of *ZGETRS* are essentially the same; consequently, the times are similar. Also, IMSL's routine does not solve for multiple right-hand sides—rather, just a solution vector. Therefore, the following code was used to make IMSL's routine equivalent to the others:

```
DO 100 IRHS = 1, NRHS
  CALL DLFSCG(..., B( 1, IRHS ), ...)
100 CONTINUE
```

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.



3.5 *DPOF, DPOTRF, F07FDF, DLFTDS*

The routines DPOF, DPOTRF, F07FDF, and DLFTDS compute the Cholesky factorization of a symmetric positive definite DOUBLE PRECISION matrix. Note that NAG's implementation of F07FDF is LAPACK's DPOTRF; consequently, the times are similar. For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.

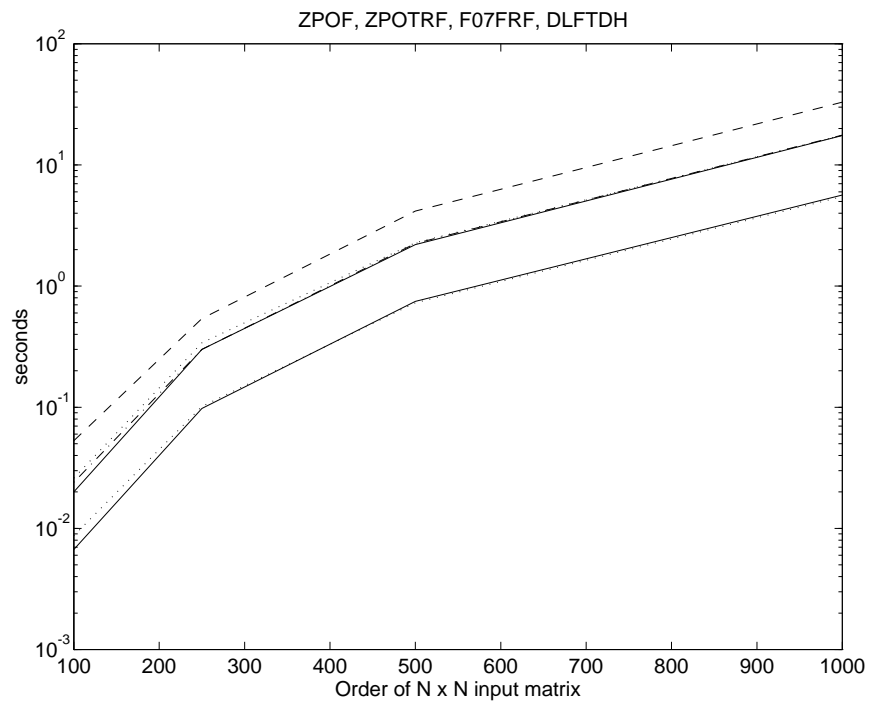
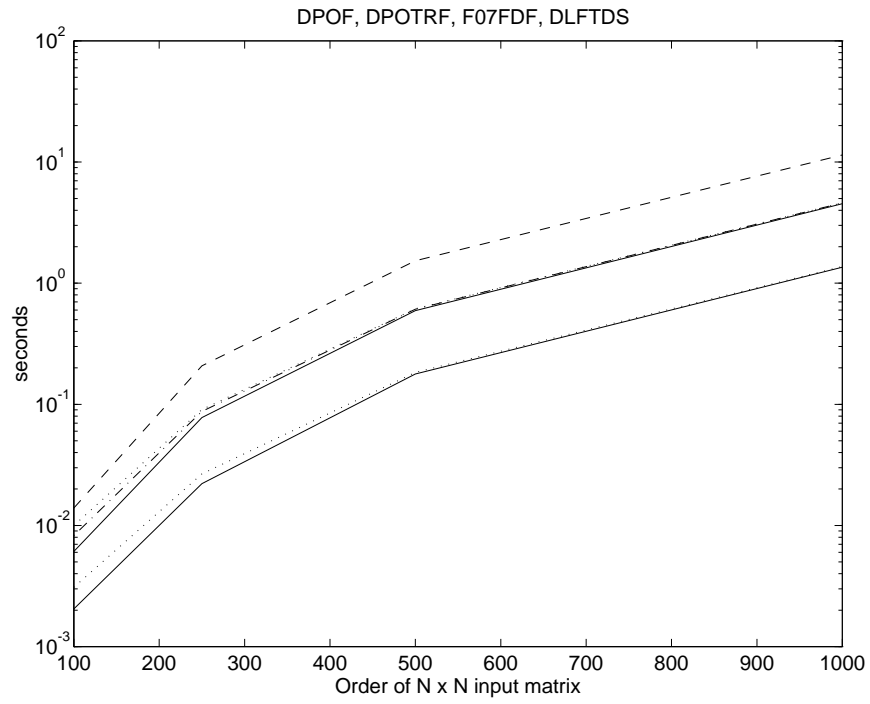
3.6 *ZPOF, ZPOTRF, F07FRF, DLFTDH*

These routines compute the Cholesky factorization of a Hermitian positive definite COMPLEX*16 matrix. Note that NAG's implementation of F07FRF is LAPACK's ZPOTRF; consequently, the times are similar. For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.



3.7 *DPOSM, DPOTRS, F07FEF, DLFSDS*

The routines *DPOSM*, *DPOTRS*, *F07FEF*, and *DLFSDS* perform a DOUBLE PRECISION triangular solve, given a solution matrix and the factorization from Section 3.5. Note that NAG's implementation of *F07FEF* is LAPACK's *DPOTRS*; consequently, the times are similar. Also, IMSL's routine does not solve for multiple right-hand sides—rather, just a solution vector. Therefore, the following code was used to make IMSL's routine equivalent to the others:

```
DO 100 IRHS = 1, NRHS
  CALL DLFSDS(..., B( 1, IRHS ), ...)
100 CONTINUE
```

For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.

3.8 *ZPOSM, ZPOTRS, F07FSF, DLFSDH*

The routines *ZPOSH*, *ZOTRS*, *F07FSF*, and *DLFSDH* do a COMPLEX*16 triangular solve, given a solution matrix and the factorization from Section 3.6. Note that NAG's implementation of *F07FSF* is LAPACK's *ZPOTRS*; consequently, the times are similar. Also, IMSL's routine does not solve for multiple right-hand sides—rather, just a solution vector. Therefore, the following code was used to make IMSL's routine equivalent to the others:

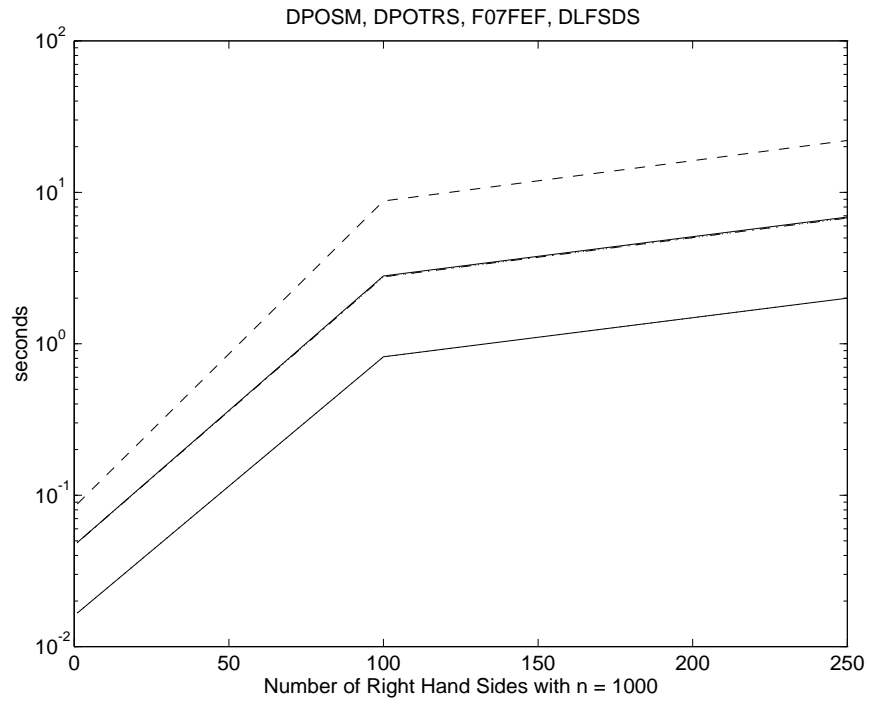
```
DO 100 IRHS = 1, NRHS
  CALL DLFSDH(..., B( 1, IRHS ), ...)
100 CONTINUE
```

For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|Ax-b\|}{\|A\|\|x\|}\epsilon$$

where ϵ is the machine precision.



3.9 DSLEV, DSPEV, F02ABF, DEVSCF

The routines DSLEV, DSPEV, F02ABF, and DEVSCF compute the eigenvalues and eigenvectors of a DOUBLE PRECISION symmetric matrix. Unlike the first 8 routines, NAG's F02ABF is *not* equivalent to LAPACK's DSPEV. Also, LAPACK and ESSL use input matrices in *packed* form, whereas NAG and IMSL do not. For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|A - ZDZ^T\|}{\|A\| * n * \epsilon} \quad \text{and} \quad \frac{\|I - ZZ^T\|}{n * \epsilon}$$

where A is the symmetric input matrix of order n . Z contains the eigenvectors, and D contains the eigenvalues. I is the identity matrix, and ϵ is the machine precision.

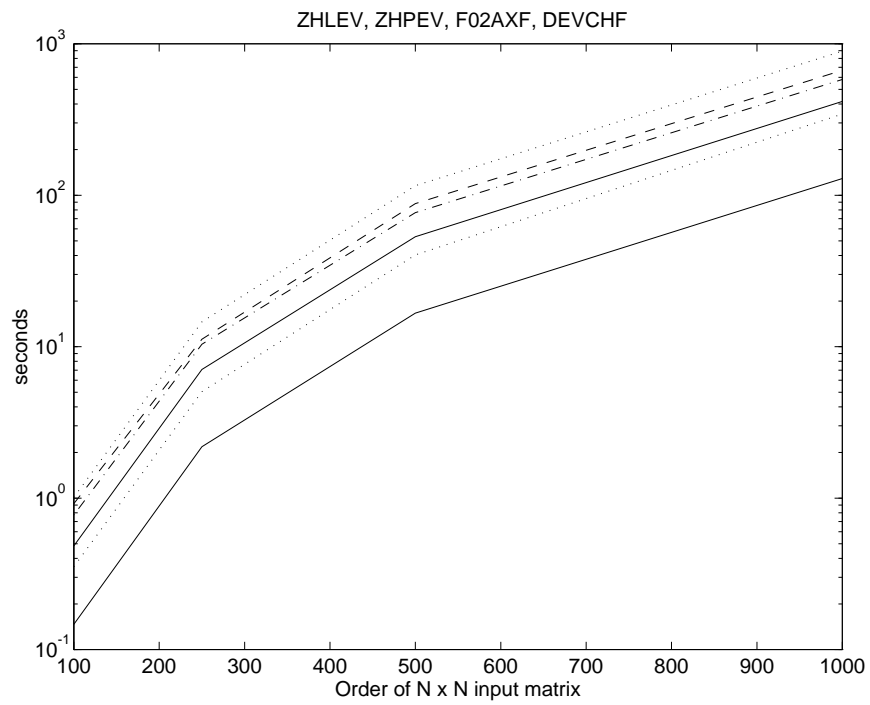
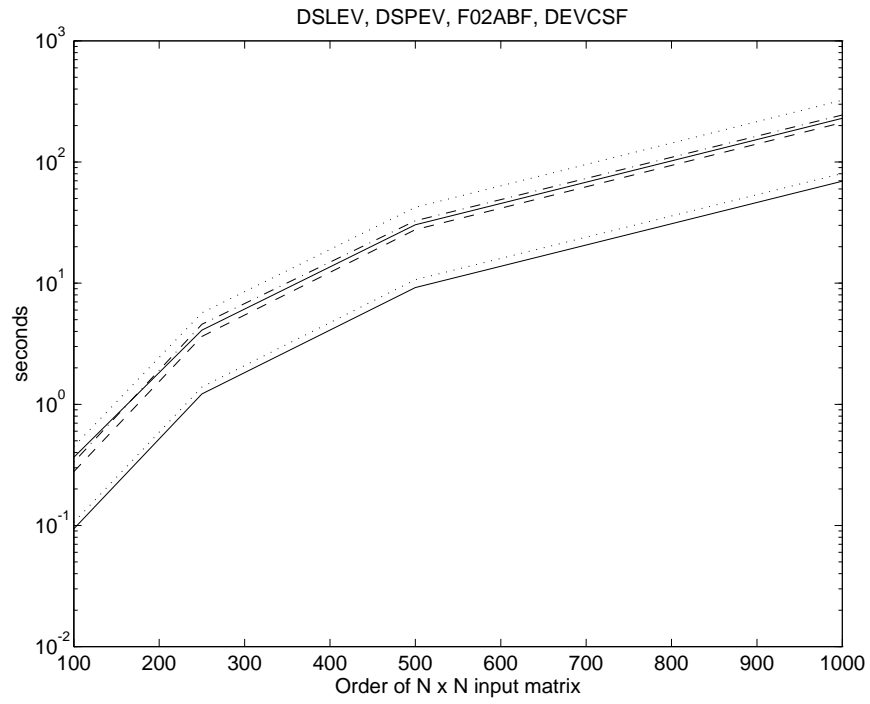
3.10 ZHLEV, ZHPEV, F02AXF, DEVCHF

These routines compute the eigenvalues and eigenvectors of a COMPLEX*16 Hermitian matrix. Unlike the first 8 routines, NAG's F02AXF is NOT equivalent to LAPACK's ZHPEV. Also, LAPACK and ESSL use input matrices in *packed* form, whereas, NAG and IMSL do not. Further, NAG accepts its input matrix as two real matrices—one to hold the real values, and the other to hold the imaginary ones. ESSL, LAPACK, and IMSL accept one complex input matrix. For uniformity, the **upper** triangle is used for all timing data.

The following test was run to validate the results:

$$\frac{\|A - ZDZ^T\|}{\|A\| * n * \epsilon} \quad \text{and} \quad \frac{\|I - ZZ^T\|}{n * \epsilon}$$

where A is the symmetric input matrix of order n . Z contains the eigenvectors, and D contains the eigenvalues. I is the identity matrix, and ϵ is the machine precision.



4 Discussion

All of the tested subroutines appear to be numerically correct on both the IBM RS/6000-550 and the new IBM RS/6000-590. Further, the ESSL subroutines achieve the overall best performance of all the packages used. Also, as a side note, the ESSL BLAS have been tested and appear error-free; better yet, they are optimized for both architectures (as most manufacturer's BLAS packages typically are). Consequently, it is recommended that the ESSL BLAS library be linked in front of the numerical analysis package of choice.

A Timing Data

The following tables are output files of the times on the IBM RS/6000-550 and RS/6000-590, respectively. Counts for Megaflops are based upon the number of operations performed in the LAPACK routines.

A.1 550.out

Numerical packages used in this timing set:

ESSL
LAPACK
NAG
IMSL

The following parameter values will be used:

N : 100 250 500 1000
NRHS : 1 100 250

Number of routine sets to be timed: 10

Start of Timings

*** Timing Set Separator ***

| | | | |
|-----------|----------------|-------------|--|
| 100 x 100 | | | |
| DGEF | .01381 seconds | 47.9 Mflops | |
| DGETRF | .02494 seconds | 26.5 Mflops | |
| F07ADF | .02035 seconds | 32.5 Mflops | |
| DLFTRG | .05011 seconds | 13.2 Mflops | |

| | | | |
|-----------|----------------|-------------|--|
| 250 x 250 | | | |
| DGEF | .17203 seconds | 60.4 Mflops | |
| DGETRF | .25225 seconds | 41.2 Mflops | |
| F07ADF | .25609 seconds | 40.6 Mflops | |
| DLFTRG | .37602 seconds | 27.6 Mflops | |

| | | | |
|-----------|-----------------|-------------|--|
| 500 x 500 | | | |
| DGEF | 1.24526 seconds | 66.8 Mflops | |
| DGETRF | 1.71697 seconds | 48.5 Mflops | |
| F07ADF | 1.80797 seconds | 46.0 Mflops | |
| DLFTRG | 2.73070 seconds | 30.5 Mflops | |

| | | | |
|-------------|------------------|-------------|--|
| 1000 x 1000 | | | |
| DGEF | 9.42146 seconds | 70.7 Mflops | |
| DGETRF | 11.64439 seconds | 57.2 Mflops | |

| | | | |
|--------|------------------|-------------|--|
| F07ADF | 12.71110 seconds | 52.4 Mflops | |
| DLFTRG | 21.34845 seconds | 31.2 Mflops | |

*** Timing Set Separator ***

| | | | |
|-----------|----------------|-------------|--|
| 100 x 100 | | | |
| ZGEF | .04310 seconds | 61.6 Mflops | |
| ZGETRF | .05652 seconds | 47.0 Mflops | |
| F07ARF | .07070 seconds | 37.6 Mflops | |
| DLFTCG | .11719 seconds | 22.7 Mflops | |

| | | | |
|-----------|-----------------|-------------|--|
| 250 x 250 | | | |
| ZGEF | .59706 seconds | 69.7 Mflops | |
| ZGETRF | .70884 seconds | 58.7 Mflops | |
| F07ARF | 1.09264 seconds | 38.1 Mflops | |
| DLFTCG | 1.53696 seconds | 27.1 Mflops | |

| | | | |
|-----------|------------------|-------------|--|
| 500 x 500 | | | |
| ZGEF | 4.55074 seconds | 73.2 Mflops | |
| ZGETRF | 5.12570 seconds | 65.0 Mflops | |
| F07ARF | 7.99196 seconds | 41.7 Mflops | |
| DLFTCG | 12.03358 seconds | 27.7 Mflops | |

| | | | |
|-------------|------------------|-------------|--|
| 1000 x 1000 | | | |
| ZGEF | 35.56992 seconds | 74.9 Mflops | |
| ZGETRF | 38.09008 seconds | 70.0 Mflops | |
| F07ARF | 60.93470 seconds | 43.7 Mflops | |
| DLFTCG | 96.09003 seconds | 27.7 Mflops | |

*** Timing Set Separator ***

| | | | |
|-------------------------------|----------------|-------------|--|
| 100 x 100 | | | |
| Number of Right Hand Sides: 1 | | | |
| DGESM | .00098 seconds | 20.3 Mflops | |
| DGETRS | .00095 seconds | 21.0 Mflops | |
| F07AEF | .00093 seconds | 21.4 Mflops | |
| DLFSRG | .00151 seconds | 13.1 Mflops | |

| | | | |
|---------------------------------|----------------|-------------|--|
| Number of Right Hand Sides: 100 | | | |
| DGESM | .03243 seconds | 61.4 Mflops | |
| DGETRS | .03545 seconds | 56.1 Mflops | |
| F07AEF | .03366 seconds | 59.1 Mflops | |
| DLFSRG | .13329 seconds | 14.9 Mflops | |

| | | | |
|---------------------------------|----------------|-------------|--|
| Number of Right Hand Sides: 250 | | | |
| DGESM | .07936 seconds | 62.7 Mflops | |

DGETRS .10037 seconds 49.6 Mflops
 F07AEF .09990 seconds 49.8 Mflops
 DLFSRG .32836 seconds 15.2 Mflops

250 x 250

Number of Right Hand Sides: 1

DGESM .00416 seconds 30.0 Mflops
 DGETRS .00454 seconds 27.5 Mflops
 F07AEF .00452 seconds 27.6 Mflops
 DLFSRG .00756 seconds 16.5 Mflops

Number of Right Hand Sides: 100

DGESM .18405 seconds 67.8 Mflops
 DGETRS .19275 seconds 64.7 Mflops
 F07AEF .20183 seconds 61.8 Mflops
 DLFSRG .72633 seconds 17.2 Mflops

Number of Right Hand Sides: 250

DGESM .44774 seconds 69.7 Mflops
 DGETRS .51719 seconds 60.3 Mflops
 F07AEF .51731 seconds 60.3 Mflops
 DLFSRG 1.85189 seconds 16.8 Mflops

500 x 500

Number of Right Hand Sides: 1

DGESM .01373 seconds 36.4 Mflops
 DGETRS .01504 seconds 33.2 Mflops
 F07AEF .01431 seconds 34.9 Mflops
 DLFSRG .02635 seconds 19.0 Mflops

Number of Right Hand Sides: 100

DGESM .70717 seconds 70.6 Mflops
 DGETRS .73682 seconds 67.8 Mflops
 F07AEF .73388 seconds 68.1 Mflops
 DLFSRG 2.65112 seconds 18.8 Mflops

Number of Right Hand Sides: 250

DGESM 1.72664 seconds 72.3 Mflops
 DGETRS 1.88323 seconds 66.3 Mflops
 F07AEF 1.88731 seconds 66.2 Mflops
 DLFSRG 6.62045 seconds 18.9 Mflops

1000 x 1000

Number of Right Hand Sides: 1

DGESM .04934 seconds 40.5 Mflops
 DGETRS .05089 seconds 39.3 Mflops
 F07AEF .05084 seconds 39.3 Mflops
 DLFSRG .11866 seconds 16.8 Mflops

Number of Right Hand Sides: 100

DGESM 2.82658 seconds 70.7 Mflops
 DGETRS 2.87006 seconds 69.7 Mflops
 F07AEF 2.87292 seconds 69.6 Mflops
 DLFSRG 10.00971 seconds 20.0 Mflops

Number of Right Hand Sides: 250

DGESM 6.80839 seconds 73.4 Mflops
 DGETRS 7.16865 seconds 69.7 Mflops
 F07AEF 7.16805 seconds 69.7 Mflops
 DLFSRG 24.98881 seconds 20.0 Mflops

*** Timing Set Separator ***

100 x 100

Number of Right Hand Sides: 1

ZGESM .00199 seconds 40.2 Mflops
 ZGETRS .00186 seconds 42.8 Mflops
 F07ASF .00185 seconds 43.1 Mflops
 DLFSCG .00360 seconds 22.2 Mflops

Number of Right Hand Sides: 100

ZGESM .11402 seconds 70.0 Mflops
 ZGETRS .11581 seconds 68.9 Mflops
 F07ASF .11489 seconds 69.5 Mflops
 DLFSCG .33419 seconds 23.9 Mflops

Number of Right Hand Sides: 250

ZGESM .27961 seconds 71.3 Mflops
 ZGETRS .30154 seconds 66.2 Mflops
 F07ASF .30331 seconds 65.8 Mflops
 DLFSCG .83361 seconds 23.9 Mflops

250 x 250

Number of Right Hand Sides: 1

ZGESM .00908 seconds 55.0 Mflops
 ZGETRS .00934 seconds 53.5 Mflops
 F07ASF .00930 seconds 53.7 Mflops
 DLFSCG .01874 seconds 26.7 Mflops

Number of Right Hand Sides: 100

ZGESM .67880 seconds 73.6 Mflops
 ZGETRS .69327 seconds 72.0 Mflops
 F07ASF .69315 seconds 72.1 Mflops
 DLFSCG 1.87768 seconds 26.6 Mflops

Number of Right Hand Sides: 250

ZGESM 1.67864 seconds 74.4 Mflops
 ZGETRS 1.75167 seconds 71.3 Mflops

F07ASF 1.75228 seconds 71.3 Mflops
 DLFSCG 4.69669 seconds 26.6 Mflops

500 x 500

Number of Right Hand Sides: 1

ZGESM .03174 seconds 63.0 Mflops
 ZGETRS .03260 seconds 61.3 Mflops
 F07ASF .03256 seconds 61.4 Mflops
 DLFSCG .07207 seconds 27.7 Mflops

Number of Right Hand Sides: 100

ZGESM 2.68238 seconds 74.5 Mflops
 ZGETRS 2.74301 seconds 72.9 Mflops
 F07ASF 2.71448 seconds 73.6 Mflops
 DLFSCG 7.15520 seconds 27.9 Mflops

Number of Right Hand Sides: 250

ZGESM 6.60774 seconds 75.6 Mflops
 ZGETRS 6.77147 seconds 73.8 Mflops
 F07ASF 6.77807 seconds 73.7 Mflops
 DLFSCG 17.91578 seconds 27.9 Mflops

1000 x 1000

Number of Right Hand Sides: 1

ZGESM .12028 seconds 66.5 Mflops
 ZGETRS .12446 seconds 64.3 Mflops
 F07ASF .12465 seconds 64.2 Mflops
 DLFSCG .29612 seconds 27.0 Mflops

Number of Right Hand Sides: 100

ZGESM 10.64363 seconds 75.1 Mflops
 ZGETRS 10.75328 seconds 74.4 Mflops
 F07ASF 10.82651 seconds 73.9 Mflops
 DLFSCG 27.78095 seconds 28.8 Mflops

Number of Right Hand Sides: 250

ZGESM 26.27937 seconds 76.1 Mflops
 ZGETRS 26.60404 seconds 75.2 Mflops
 F07ASF 26.60625 seconds 75.2 Mflops
 DLFSCG 69.50199 seconds 28.8 Mflops

*** Timing Set Separator ***

100 x 100

DPOF .00610 seconds 55.5 Mflops
 DPOTRF .01000 seconds 33.8 Mflops
 F07FDF .00825 seconds 41.0 Mflops
 DLFTDS .01395 seconds 24.2 Mflops

250 x 250

DPOF .07776 seconds 67.4 Mflops
 DPOTRF .09048 seconds 57.9 Mflops
 F07FDF .08737 seconds 60.0 Mflops
 DLFTDS .20766 seconds 25.2 Mflops

500 x 500

DPOF .59384 seconds 70.4 Mflops
 DPOTRF .61534 seconds 67.9 Mflops
 F07FDF .60912 seconds 68.6 Mflops
 DLFTDS 1.53247 seconds 27.3 Mflops

1000 x 1000

DPOF 4.52868 seconds 73.7 Mflops
 DPOTRF 4.61709 seconds 72.3 Mflops
 F07FDF 4.60352 seconds 72.5 Mflops
 DLFTDS 11.43321 seconds 29.2 Mflops

*** Timing Set Separator ***

100 x 100

ZPOF .01926 seconds 70.8 Mflops
 ZPOTRF .02563 seconds 53.2 Mflops
 F07FRF .02449 seconds 55.7 Mflops
 DLFTDH .05344 seconds 25.5 Mflops

250 x 250

ZPOF .28881 seconds 72.8 Mflops
 ZPOTRF .33835 seconds 62.1 Mflops
 F07FRF .30192 seconds 69.6 Mflops
 DLFTDH .54172 seconds 38.8 Mflops

500 x 500

ZPOF 2.22075 seconds 75.4 Mflops
 ZPOTRF 2.28085 seconds 73.4 Mflops
 F07FRF 2.24692 seconds 74.5 Mflops
 DLFTDH 4.15906 seconds 40.3 Mflops

1000 x 1000

ZPOF 17.47949 seconds 76.5 Mflops
 ZPOTRF 17.60942 seconds 75.9 Mflops
 F07FRF 17.63009 seconds 75.8 Mflops
 DLFTDH 33.04114 seconds 40.4 Mflops

*** Timing Set Separator ***

100 x 100
 Number of Right Hand Sides: 1
 DPOSM .00069 seconds 28.9 Mflops
 DPOTRS .00071 seconds 28.3 Mflops
 F07FEF .00067 seconds 29.7 Mflops
 DLFSDS .00118 seconds 17.0 Mflops
 Number of Right Hand Sides: 100
 DPOSM .03128 seconds 63.9 Mflops
 DPOTRS .03120 seconds 64.1 Mflops
 F07FEF .03115 seconds 64.2 Mflops
 DLFSDS .11143 seconds 17.9 Mflops
 Number of Right Hand Sides: 250
 DPOSM .07549 seconds 66.2 Mflops
 DPOTRS .07571 seconds 66.0 Mflops
 F07FEF .07523 seconds 66.5 Mflops
 DLFSDS .27968 seconds 17.9 Mflops

250 x 250
 Number of Right Hand Sides: 1
 DPOSM .00380 seconds 32.9 Mflops
 DPOTRS .00394 seconds 31.7 Mflops
 F07FEF .00371 seconds 33.7 Mflops
 DLFSDS .00656 seconds 19.0 Mflops
 Number of Right Hand Sides: 100
 DPOSM .17960 seconds 69.6 Mflops
 DPOTRS .17742 seconds 70.5 Mflops
 F07FEF .17874 seconds 69.9 Mflops
 DLFSDS .65458 seconds 19.1 Mflops
 Number of Right Hand Sides: 250
 DPOSM .43529 seconds 71.8 Mflops
 DPOTRS .43542 seconds 71.8 Mflops
 F07FEF .43321 seconds 72.1 Mflops
 DLFSDS 1.63897 seconds 19.1 Mflops

500 x 500
 Number of Right Hand Sides: 1
 DPOSM .01336 seconds 37.4 Mflops
 DPOTRS .01334 seconds 37.5 Mflops
 F07FEF .01315 seconds 38.0 Mflops
 DLFSDS .02355 seconds 21.2 Mflops
 Number of Right Hand Sides: 100

DPOSM .69936 seconds 71.5 Mflops
 DPOTRS .69738 seconds 71.7 Mflops
 F07FEF .69636 seconds 71.8 Mflops
 DLFSDS 2.41227 seconds 20.7 Mflops
 Number of Right Hand Sides: 250
 DPOSM 1.70554 seconds 73.3 Mflops
 DPOTRS 1.70593 seconds 73.3 Mflops
 F07FEF 1.70174 seconds 73.5 Mflops
 DLFSDS 5.93529 seconds 21.1 Mflops

1000 x 1000
 Number of Right Hand Sides: 1
 DPOSM .04870 seconds 41.1 Mflops
 DPOTRS .04843 seconds 41.3 Mflops
 F07FEF .04851 seconds 41.2 Mflops
 DLFSDS .08741 seconds 22.9 Mflops
 Number of Right Hand Sides: 100
 DPOSM 2.80515 seconds 71.3 Mflops
 DPOTRS 2.76205 seconds 72.4 Mflops
 F07FEF 2.76806 seconds 72.3 Mflops
 DLFSDS 8.77114 seconds 22.8 Mflops
 Number of Right Hand Sides: 250
 DPOSM 6.87006 seconds 72.8 Mflops
 DPOTRS 6.75116 seconds 74.1 Mflops
 F07FEF 6.75768 seconds 74.0 Mflops
 DLFSDS 21.99848 seconds 22.7 Mflops

*** Timing Set Separator ***

100 x 100
 Number of Right Hand Sides: 1
 ZPOSM .00171 seconds 47.1 Mflops
 ZPOTRS .00188 seconds 42.7 Mflops
 F07FSF .00167 seconds 48.2 Mflops
 DLFS DH .00381 seconds 21.1 Mflops
 Number of Right Hand Sides: 100
 ZPOSM .11168 seconds 72.0 Mflops
 ZPOTRS .11189 seconds 71.9 Mflops
 F07FSF .11170 seconds 72.0 Mflops
 DLFS DH .35981 seconds 22.3 Mflops
 Number of Right Hand Sides: 250
 ZPOSM .27350 seconds 73.5 Mflops
 ZPOTRS .27320 seconds 73.6 Mflops
 F07FSF .27353 seconds 73.5 Mflops

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DLFSDH      .90033 seconds  22.3 Mflops

      250 x   250
      Number of Right Hand Sides:    1
ZPOSM       .01001 seconds  50.1 Mflops
ZPOTRS      .00903 seconds  55.5 Mflops
F07FSF      .00900 seconds  55.7 Mflops
DLFSDH      .02047 seconds  24.5 Mflops
      Number of Right Hand Sides:   100
ZPOSM       .67220 seconds  74.5 Mflops
ZPOTRS      .67288 seconds  74.5 Mflops
F07FSF      .67110 seconds  74.7 Mflops
DLFSDH      2.04851 seconds  24.5 Mflops
      Number of Right Hand Sides:   250
ZPOSM       1.65947 seconds  75.5 Mflops
ZPOTRS      1.66043 seconds  75.4 Mflops
F07FSF      1.65710 seconds  75.6 Mflops
DLFSDH      5.19694 seconds  24.1 Mflops

      500 x   500
      Number of Right Hand Sides:    1
ZPOSM       .03274 seconds  61.2 Mflops
ZPOTRS      .03290 seconds  60.9 Mflops
F07FSF      .03435 seconds  58.3 Mflops
DLFSDH      .07759 seconds  25.8 Mflops
      Number of Right Hand Sides:   100
ZPOSM       2.67634 seconds  74.8 Mflops
ZPOTRS      2.67118 seconds  74.9 Mflops
F07FSF      2.66576 seconds  75.1 Mflops
DLFSDH      8.20426 seconds  24.4 Mflops
      Number of Right Hand Sides:   250
ZPOSM       6.64089 seconds  75.4 Mflops
ZPOTRS      6.62695 seconds  75.5 Mflops
F07FSF      6.57015 seconds  76.2 Mflops
DLFSDH     19.32584 seconds  25.9 Mflops

      1000 x  1000
      Number of Right Hand Sides:    1
ZPOSM       .12407 seconds  64.5 Mflops
ZPOTRS      .12392 seconds  64.6 Mflops
F07FSF      .12514 seconds  64.0 Mflops
DLFSDH      .29777 seconds  26.9 Mflops
      Number of Right Hand Sides:   100
ZPOSM      10.60525 seconds  75.5 Mflops

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ZPOTRS     10.60409 seconds  75.5 Mflops
F07FSF     10.59904 seconds  75.5 Mflops
DLFSDH     29.74984 seconds  26.9 Mflops
      Number of Right Hand Sides:   250
ZPOSM      26.29174 seconds  76.1 Mflops
ZPOTRS     26.22856 seconds  76.3 Mflops
F07FSF     26.25879 seconds  76.2 Mflops
DLFSDH     74.42543 seconds  26.9 Mflops

*** Timing Set Separator ***

      100 x   100
DSLEV       .36523 seconds  21.7 Mflops
DSPEV       .44989 seconds  17.6 Mflops
F02ABF      .33433 seconds  23.7 Mflops
DEVCSF      .27842 seconds  28.5 Mflops

      250 x   250
DSLEV       4.10146 seconds  28.7 Mflops
DSPEV       5.70087 seconds  20.6 Mflops
F02ABF      4.57444 seconds  25.7 Mflops
DEVCSF      3.63383 seconds  32.4 Mflops

      500 x   500
DSLEV      30.30769 seconds  30.1 Mflops
DSPEV      42.34420 seconds  21.5 Mflops
F02ABF     32.73366 seconds  27.9 Mflops
DEVCSF     27.66989 seconds  33.0 Mflops

      1000 x  1000
DSLEV     229.48141 seconds  31.1 Mflops
DSPEV     323.34836 seconds  22.1 Mflops
F02ABF   244.58197 seconds  29.2 Mflops
DEVCSF   211.76927 seconds  33.8 Mflops

*** Timing Set Separator ***

      100 x   100
ZHLEV       .48390 seconds  37.4 Mflops
ZHPEV       1.01247 seconds  17.9 Mflops
F02AXF      .77370 seconds  23.4 Mflops
DEVCHF      .91984 seconds  19.7 Mflops

      250 x   250

```

| | | | | |
|--------|----------|---------|------|--------|
| ZHLEV | 7.06681 | seconds | 38.5 | Mflops |
| ZHPEV | 14.56624 | seconds | 18.7 | Mflops |
| FO2AXF | 10.37188 | seconds | 26.3 | Mflops |
| DEVCHF | 11.19001 | seconds | 24.3 | Mflops |

500 x 500

| | | | | |
|--------|-----------|---------|------|--------|
| ZHLEV | 53.18078 | seconds | 41.4 | Mflops |
| ZHPEV | 115.52283 | seconds | 19.1 | Mflops |
| FO2AXF | 76.70922 | seconds | 28.7 | Mflops |
| DEVCHF | 87.96585 | seconds | 25.0 | Mflops |

1000 x 1000

| | | | | |
|--------|-----------|---------|------|--------|
| ZHLEV | 415.99728 | seconds | 41.4 | Mflops |
| ZHPEV | 895.60843 | seconds | 19.2 | Mflops |
| FO2AXF | 580.77693 | seconds | 29.7 | Mflops |
| DEVCHF | 668.79005 | seconds | 25.8 | Mflops |

End of Timings

A.2 590.out

Numerical packages used in this timing set:

ESSL

LAPACK

The following parameter values will be used:

N : 100 250 500 1000

NRHS : 1 100 250

Number of routine sets to be timed: 10

Start of Timings

*** Timing Set Separator ***

100 x 100

DGEF .00444 seconds 148.9 Mflops

DGETRF .00753 seconds 87.9 Mflops

250 x 250

DGEF .04951 seconds 209.7 Mflops

DGETRF .06439 seconds 161.3 Mflops

500 x 500

DGEF .37139 seconds 224.0 Mflops

DGETRF .48771 seconds 170.6 Mflops

1000 x 1000

DGEF 2.79424 seconds 238.4 Mflops

DGETRF 3.85433 seconds 172.8 Mflops

*** Timing Set Separator ***

100 x 100

ZGEF .01348 seconds 197.1 Mflops

ZGETRF .01794 seconds 148.1 Mflops

250 x 250

ZGEF .18206 seconds 228.5 Mflops

ZGETRF .21470 seconds 193.8 Mflops

500 x 500

ZGEF 1.37634 seconds 242.0 Mflops

ZGETRF 1.60849 seconds 207.1 Mflops

1000 x 1000

ZGEF 10.70659 seconds 249.0 Mflops

ZGETRF 12.22530 seconds 218.0 Mflops

*** Timing Set Separator ***

100 x 100

Number of Right Hand Sides: 1

DGESM .00034 seconds 58.0 Mflops

DGETRS .00032 seconds 61.6 Mflops

Number of Right Hand Sides: 100

DGESM .00921 seconds 216.0 Mflops

DGETRS .00907 seconds 219.5 Mflops

Number of Right Hand Sides: 250

DGESM .02303 seconds 216.0 Mflops

DGETRS .02276 seconds 218.6 Mflops

250 x 250

Number of Right Hand Sides: 1

DGESM .00130 seconds 95.9 Mflops

DGETRS .00163 seconds 76.6 Mflops

Number of Right Hand Sides: 100

DGESM .05454 seconds 228.7 Mflops

DGETRS .05426 seconds 229.9 Mflops

Number of Right Hand Sides: 250

DGESM .13310 seconds 234.3 Mflops

DGETRS .13962 seconds 223.4 Mflops

500 x 500

Number of Right Hand Sides: 1

DGESM .00505 seconds 98.9 Mflops

DGETRS .00535 seconds 93.4 Mflops

Number of Right Hand Sides: 100

DGESM .20915 seconds 238.8 Mflops

DGETRS .21124 seconds 236.5 Mflops

Number of Right Hand Sides: 250

DGESM .51023 seconds 244.7 Mflops

DGETRS .53649 seconds 232.8 Mflops

1000 x 1000

Number of Right Hand Sides: 1

DGESM .01743 seconds 114.7 Mflops

DGETRS .01841 seconds 108.6 Mflops

Number of Right Hand Sides: 100

DGESM .82599 seconds 242.0 Mflops
 DGETRS .84246 seconds 237.3 Mflops
 Number of Right Hand Sides: 250
 DGESM 2.01335 seconds 248.2 Mflops
 DGETRS 2.09311 seconds 238.8 Mflops

*** Timing Set Separator ***

100 x 100
 Number of Right Hand Sides: 1
 ZGESM .00075 seconds 105.8 Mflops
 ZGETRS .00075 seconds 106.0 Mflops
 Number of Right Hand Sides: 100
 ZGESM .04781 seconds 166.9 Mflops
 ZGETRS .04794 seconds 166.5 Mflops
 Number of Right Hand Sides: 250
 ZGESM .11915 seconds 167.4 Mflops
 ZGETRS .11995 seconds 166.3 Mflops

250 x 250
 Number of Right Hand Sides: 1
 ZGESM .00368 seconds 135.7 Mflops
 ZGETRS .00389 seconds 128.3 Mflops
 Number of Right Hand Sides: 100
 ZGESM .24832 seconds 201.2 Mflops
 ZGETRS .24924 seconds 200.4 Mflops
 Number of Right Hand Sides: 250
 ZGESM .61376 seconds 203.5 Mflops
 ZGETRS .62532 seconds 199.7 Mflops

500 x 500
 Number of Right Hand Sides: 1
 ZGESM .01323 seconds 151.1 Mflops
 ZGETRS .01370 seconds 145.9 Mflops
 Number of Right Hand Sides: 100
 ZGESM .89052 seconds 224.5 Mflops
 ZGETRS .94063 seconds 212.5 Mflops
 Number of Right Hand Sides: 250
 ZGESM 2.20119 seconds 227.0 Mflops
 ZGETRS 2.23438 seconds 223.7 Mflops

1000 x 1000
 Number of Right Hand Sides: 1
 ZGESM .04983 seconds 160.5 Mflops

ZGETRS .05070 seconds 157.7 Mflops
 Number of Right Hand Sides: 100
 ZGESM 3.36467 seconds 237.7 Mflops
 ZGETRS 3.38821 seconds 236.1 Mflops
 Number of Right Hand Sides: 250
 ZGESM 8.30722 seconds 240.7 Mflops
 ZGETRS 8.43493 seconds 237.1 Mflops

*** Timing Set Separator ***

100 x 100
 DPOF .00205 seconds 164.8 Mflops
 DPOTRF .00309 seconds 109.5 Mflops

250 x 250
 DPOF .02216 seconds 236.4 Mflops
 DPOTRF .02668 seconds 196.4 Mflops

500 x 500
 DPOF .17797 seconds 234.8 Mflops
 DPOTRF .18328 seconds 228.0 Mflops

1000 x 1000
 DPOF 1.35571 seconds 246.2 Mflops
 DPOTRF 1.37470 seconds 242.8 Mflops

*** Timing Set Separator ***

100 x 100
 ZPOF .00672 seconds 202.8 Mflops
 ZPOTRF .00871 seconds 156.5 Mflops

250 x 250
 ZPOF .09775 seconds 215.1 Mflops
 ZPOTRF .10162 seconds 206.9 Mflops

500 x 500
 ZPOF .74767 seconds 223.9 Mflops
 ZPOTRF .72744 seconds 230.1 Mflops

1000 x 1000
 ZPOF 5.63974 seconds 236.9 Mflops
 ZPOTRF 5.47636 seconds 244.0 Mflops

*** Timing Set Separator ***

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100 x 100
  Number of Right Hand Sides: 1
DPOSM .00023 seconds 85.9 Mflops
DPOTRS .00023 seconds 85.6 Mflops
  Number of Right Hand Sides: 100
DPOSM .00854 seconds 234.2 Mflops
DPOTRS .00851 seconds 235.1 Mflops
  Number of Right Hand Sides: 250
DPOSM .02121 seconds 235.8 Mflops
DPOTRS .02139 seconds 233.8 Mflops

250 x 250
  Number of Right Hand Sides: 1
DPOSM .00126 seconds 99.1 Mflops
DPOTRS .00125 seconds 99.8 Mflops
  Number of Right Hand Sides: 100
DPOSM .05260 seconds 237.7 Mflops
DPOTRS .05256 seconds 237.8 Mflops
  Number of Right Hand Sides: 250
DPOSM .12891 seconds 242.4 Mflops
DPOTRS .12849 seconds 243.2 Mflops

500 x 500
  Number of Right Hand Sides: 1
DPOSM .00469 seconds 106.6 Mflops
DPOTRS .00460 seconds 108.8 Mflops
  Number of Right Hand Sides: 100
DPOSM .20583 seconds 242.9 Mflops
DPOTRS .20610 seconds 242.6 Mflops
  Number of Right Hand Sides: 250
DPOSM .50275 seconds 248.6 Mflops
DPOTRS .50278 seconds 248.6 Mflops

1000 x 1000
  Number of Right Hand Sides: 1
DPOSM .01666 seconds 120.0 Mflops
DPOTRS .01669 seconds 119.8 Mflops
  Number of Right Hand Sides: 100
DPOSM .82002 seconds 243.9 Mflops
DPOTRS .82039 seconds 243.8 Mflops
  Number of Right Hand Sides: 250
DPOSM 2.00066 seconds 249.9 Mflops

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DPOTRS 2.00077 seconds 249.9 Mflops

*** Timing Set Separator ***

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100 x 100
  Number of Right Hand Sides: 1
ZPOSM .00068 seconds 118.9 Mflops
ZPOTRS .00068 seconds 118.4 Mflops
  Number of Right Hand Sides: 100
ZPOSM .04690 seconds 171.4 Mflops
ZPOTRS .04699 seconds 171.1 Mflops
  Number of Right Hand Sides: 250
ZPOSM .11626 seconds 172.9 Mflops
ZPOTRS .11628 seconds 172.9 Mflops

250 x 250
  Number of Right Hand Sides: 1
ZPOSM .00350 seconds 143.3 Mflops
ZPOTRS .00346 seconds 144.8 Mflops
  Number of Right Hand Sides: 100
ZPOSM .24578 seconds 203.8 Mflops
ZPOTRS .24638 seconds 203.3 Mflops
  Number of Right Hand Sides: 250
ZPOSM .60861 seconds 205.8 Mflops
ZPOTRS .60818 seconds 205.9 Mflops

500 x 500
  Number of Right Hand Sides: 1
ZPOSM .01284 seconds 155.9 Mflops
ZPOTRS .01286 seconds 155.7 Mflops
  Number of Right Hand Sides: 100
ZPOSM .88620 seconds 225.9 Mflops
ZPOTRS .88635 seconds 225.9 Mflops
  Number of Right Hand Sides: 250
ZPOSM 2.18976 seconds 228.6 Mflops
ZPOTRS 2.19077 seconds 228.5 Mflops

1000 x 1000
  Number of Right Hand Sides: 1
ZPOSM .04790 seconds 167.1 Mflops
ZPOTRS .04784 seconds 167.3 Mflops
  Number of Right Hand Sides: 100
ZPOSM 3.35386 seconds 238.7 Mflops
ZPOTRS 3.35393 seconds 238.6 Mflops

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Number of Right Hand Sides: 250
ZPOSM 8.27809 seconds 241.7 Mflops
ZPOTRS 8.28052 seconds 241.7 Mflops

*** Timing Set Separator ***

100 x 100
DSLEV .09377 seconds 84.7 Mflops
DSPEV .10606 seconds 74.9 Mflops

250 x 250
DSLEV 1.21790 seconds 96.7 Mflops
DSPEV 1.38857 seconds 84.8 Mflops

500 x 500
DSLEV 9.18926 seconds 99.3 Mflops
DSPEV 10.68463 seconds 85.4 Mflops

1000 x 1000
DSLEV 69.46343 seconds 102.9 Mflops
DSPEV 80.43700 seconds 88.9 Mflops

*** Timing Set Separator ***

100 x 100
ZHLEV .14683 seconds 123.2 Mflops
ZHPEV .35243 seconds 51.3 Mflops

250 x 250
ZHLEV 2.18221 seconds 124.8 Mflops
ZHPEV 5.04441 seconds 54.0 Mflops

500 x 500
ZHLEV 16.64748 seconds 132.3 Mflops
ZHPEV 40.33818 seconds 54.6 Mflops

1000 x 1000
ZHLEV 128.84442 seconds 133.8 Mflops
ZHPEV 343.85137 seconds 50.1 Mflops

End of Timings